

Inequalities with negative numbers

1 Complete the workings to solve the equation and inequality.

$17 - 4x = 9$
 $\quad + 4x$ $\left\{ \begin{array}{l} \square \\ \square \\ \square \end{array} \right. = 9 + 4x$ $\left\{ \begin{array}{l} + 4x \\ - 9 \\ \square \end{array} \right.$
 $\square = \square$
 $\square = \square$

$17 - 4x > 9$
 $\quad + 4x$ $\left\{ \begin{array}{l} \square \\ \square \\ \square \end{array} \right. \circ 9 + 4x$ $\left\{ \begin{array}{l} + 4x \\ - 9 \\ \square \end{array} \right.$
 $\square \circ \square$
 $\square \circ \square$

2 Match the inequalities to the solutions.

$5x - 8 > 56$

$x \leq 6\frac{3}{8}$

$56 - 5x < 8$

$x > 12\frac{4}{5}$

$8x - 5 \leq 56$

$x \leq 7\frac{5}{8}$

$5 \leq 56 - 8x$

$x > 9\frac{3}{5}$

3 Amir, Jack and Rosie have attempted to solve $40 - 3x \leq 10$
Find their mistakes and correct them.

Amir

$$\begin{array}{l} 40 - 3x \leq 10 \\ -3x \leq -30 \\ x \leq 10 \end{array}$$

Jack

$$\begin{array}{l} 40 - 3x \leq 10 \\ -3x \leq -30 \\ x > 10 \end{array}$$

Rosie

$$\begin{array}{l} 40 - 3x \leq 10 \\ 40 \leq 10 + 3x \\ 30 \leq 3x \\ 10 \leq x \\ x \leq 10 \end{array}$$

Whose method do you prefer?

Explain your choice to a partner.

4 Solve the inequalities.

a) $-\frac{1}{2}x > 45$

d) $-49 < -7x$

b) $-5x + 24 < 54$

e) $-x - 5 \geq 20$

c) $15 \geq 30 - \frac{1}{2}x$

f) $12 - \frac{x}{3} > -10$

5 Rosie solves $3(2 - x) > 15$ and $24 > 12(3 - 2x)$ using two different methods.

a) Complete her workings.

Method 1

$$\begin{array}{l}
 3(2 - x) > 15 \\
 6 - 3x > 15 \\
 \underline{\hspace{2cm}} \\
 \underline{\hspace{2cm}} \\
 \underline{\hspace{2cm}}
 \end{array}$$

Method 2

$$\begin{array}{l}
 24 > 12(3 - 2x) \\
 2 > 3 - 2x \\
 \underline{\hspace{2cm}} \\
 \underline{\hspace{2cm}} \\
 \underline{\hspace{2cm}}
 \end{array}$$

b) Use your preferred method to solve $24 > 5(13 - 4x)$.

Compare your choice of method with a partner's.



6 Solve the inequalities.

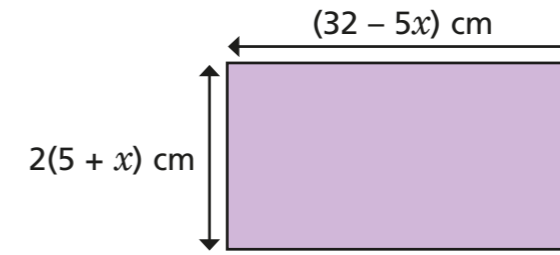
a) $3(4 - x) > 30$

c) $100 > 10(4 - x)$

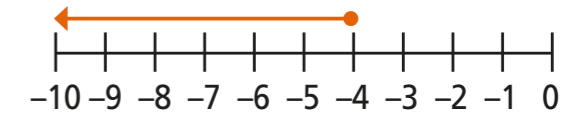
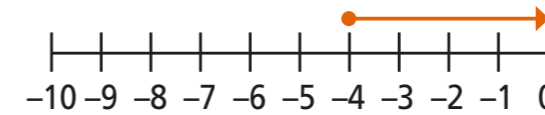
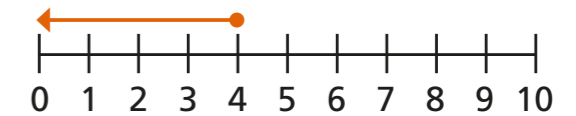
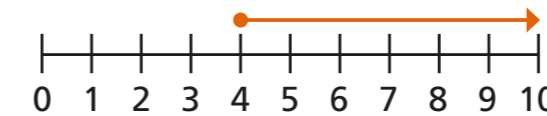
b) $2(x + 13) < 14$

d) $-2(x + 5) > 16$

7 The perimeter of the rectangle is greater than 63 cm.
If x is an integer, what is the largest possible value of x ?



8 Which number line represents the solution to $1 \leq 9 - 2x$? Tick your answer.



9 Find a value of p that satisfies both of the inequalities.

$$p - 7 > -4 \quad \text{and} \quad 2p - 7 < 5$$

Compare answers with a partner.

